

1. Find the limit:

$$(a) \lim_{x \rightarrow \infty} \sqrt{x} \quad (b) \lim_{x \rightarrow 1^+} \frac{1}{\ln(x)} - \frac{1}{x-1} \quad (c) \lim_{x \rightarrow -\infty} x^2 e^x \quad (d) \lim_{x \rightarrow 1} \frac{2-x}{(x-1)^2}$$

$$(e) \lim_{x \rightarrow 5^-} \frac{-6}{x-5} \quad (f) \lim_{x \rightarrow \infty} \frac{x^3 - 2x + 3}{5x^2 - 2x^3} \quad (g) \lim_{x \rightarrow 4} \frac{x-4}{|4-x|}$$

2. Find y' :

$$(a) y = \ln(\sinh(x)) \quad (b) y = \sqrt{x} e^{\cosh(3x)} \quad (c) y = (1+x^2) \arctan(x) \quad (d) y = x \ln(\tan^{-1}(x))$$

$$(e) y = 5^{-1/x} \quad (f) y = x^{\sin(x)} \quad (g) y = \log_{10}(x^2 - 4) \quad (h) y = \sqrt{1 + 2e^{3x}}$$

$$(i) y = \ln(x^2 + y^2) \quad (j) y = \int_{1/x^2}^0 \sin^3(t) dt \quad (k) y = \frac{\ln(x)}{e^x}$$

3. Find the exact value of: (a) $\arcsin(-1/\sqrt{2})$ (b) $\cos(\sin^{-1}(x))$

4. A bacteria culture initially contains 10 cells and grows at a rate proportional to its size. After an hour the population has increased to 106. (a) Find an expression for the number of bacteria after t hours. (b) When will the population reach 10,000 cells?

5. (a) Find f^{-1} given $f(x) = \frac{1 - \sqrt{x}}{1 + \sqrt{x}}$ (b) Find $(f^{-1})'(1)$ given $f(x) = x^3 + x + 1$.

6. Evaluate the integral:

$$(a) \int \frac{e^x}{e^{2x} + 1} dx \quad (b) \int \frac{dx}{x + \sqrt{x}} \quad (c) \int \sec(x) dx \quad (d) \int \frac{dx}{\sec(x) + \tan(x)}$$

$$(e) \int_{-1}^1 e^{|x|} dx \quad (f) \int \frac{x}{\sqrt{x^2 + 1}} dx \quad (g) \int \frac{dx}{x \cos(\ln(x))}$$

7. (a) Find an approximation to the integral $\int_1^2 x^2 dx$ using a Riemann sum with a regular partition with left endpoints and $n = 4$.

(b) Given that

$$\sum_{i=1}^n i = \frac{n(n+1)}{2}, \quad \sum_{i=1}^n i^2 = \frac{n(n+1)(2n+1)}{6}, \quad \text{and} \quad \sum_{i=1}^n i^3 = \left[\frac{n(n+1)}{2} \right]^2.$$

Use the limit definition of the integral, with right endpoints and a regular partition, to find the exact value of $\int_1^2 x^2 dx$.

8. If 1200 cm² of material is available to make a box with a square base and an open top, find the largest possible volume of the box.

9. Complete two iterations of Newton's Method to approximate a root of $y = 3x^2 - 2$ using an initial guess of $x_1 = 1$.

10. Given that $y = x - 3x^{1/3}$, $y' = 1 - \frac{1}{x^{2/3}}$, $y'' = \frac{2}{3x^{5/3}}$

(a) State the domain of the function, does the function have any vertical or horizontal asymptotes?

(b) Determine the intervals where y is increasing and decreasing.

(c) Determine the intervals where y is concave up and concave down.

(d) Find any local maximum or minimum values.

(e) Sketch the graph of the function.

11. Given that $f(x) = \frac{x^2 - x}{x^2 + x - 2}$, $f'(x) = \frac{2}{(x + 2)^2}$, $f''(x) = \frac{-4}{(x + 2)^3}$
- State the domain of the function, does the function have any vertical or horizontal asymptotes?
 - Determine the intervals where y is increasing and decreasing.
 - Determine the intervals where y is concave up and concave down.
 - Find any local maximum or minimum values.
 - Sketch the graph of the function.
12. (a) State the Intermediate Value Theorem
 (b) State Rolle's Theorem.
 (c) State the Mean Value Theorem.
 (d) Find all numbers c that satisfy the conclusion of the Mean Value Theorem for $f(x) = \ln(x)$ on the interval $[e, e^2]$
13. Find the absolute maximum and absolute minimum values of $f(x) = \cosh(x)$ over the interval $[\ln(1/2), \ln(3)]$.
14. A balloon is rising at a constant rate of 5 ft/s. A boy is cycling along a straight road at a speed of 15 ft/s. When he passes under the balloon, it is 45 ft above him. How fast is the distance between the boy and the balloon increasing 3 s later?
15. The radius of a circular disk was found to be 24 cm with a possible error in measurement of 0.2 cm. Use differentials to estimate the error, relative error, and percentage error in computing the area of the disk
16. Find the linearization of $f(x) = e^x$ at the point $a = 1/2$, and then use this linearization to approximate e . (Hint: $\ln(1.6) \approx 1/2$)
17. If a particle has position function $s(t) = t^3 - 12t + 3$, where $t \geq 0$ is measured in seconds and s in feet.
- Find the velocity and acceleration function.
 - When is the particle moving forward and when is it moving backward?
 - Find the total distance traveled in the first 3 seconds.
18. Use the limit definition of the derivative to find $f'(x)$ given $f(x) = \sqrt{1 + 2x}$.
19. Find a and b so that
- $$f(x) = \begin{cases} ax^3, & x \leq 2 \\ x^2 + b, & x > 2 \end{cases}$$
- is differentiable everywhere.
20. Given $f(x) = \frac{1}{x^2}$ and $g(x) = \sqrt{x}$ find g/f , $f \circ f$ and $g \circ f$ and state their domains.