

What is area of annular strip?

$$\text{Area}_{\text{strip}} = \text{Area}_{\text{wedge}_1} - \text{Area}_{\text{wedge}_2}$$

So what is area of wedge?



$$\text{Area of circle} = \pi r^2$$

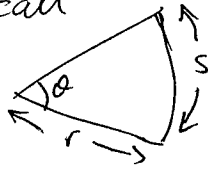
so area of wedge = fraction of πr^2 proportional to θ

$$= \left(\frac{\theta}{2\pi}\right) \pi r^2$$

$$= \frac{\theta}{2} r^2$$

$$\Rightarrow \text{Area of strip} = \frac{\theta}{2} [r_1^2 - r_2^2] = \frac{\theta}{2} (r_1 - r_2)(r_1 + r_2)$$

Recall



$$\text{Arc length } s = r\theta$$

$$\text{so Area} = (r_1 - r_2) \frac{r_1\theta + r_2\theta}{2}$$

$$= (r_1 - r_2) \frac{s_1 + s_2}{2}$$

$$= L \left(\frac{s_1 + s_2}{2}\right)$$

