

# Differential Dynamical Systems

## Errata (First Printing)

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### **Abstract**

Errors are listed by page and line number. The symbol  $\implies$  means “replace with”. A negative line number means count from the bottom of the page. Equation lines are counted as one line.

Note that the first printing has 10 9 8 7 6 5 4 3 2 1 on the copyright page. The second printing should be out in early 2009, and will have 10 9 8 7 6 5 4 3 2 on the copyright page.

Chap.	Page	Line	Change	Thanks to
1	2	5	“(fluent quantities)” $\implies$ “(fluxions)”	SS
	2	9	“find the fluxions” $\implies$ “find the fluent quantities”	SS
	7	-3	“bounded sequence has a” $\implies$ “bounded function has a”	SS
	10	-5	“These equations are linear” $\implies$ “These equations are affine”	
	10	-4,-3	“then the equations of motion are not linear but are affine, see Exercise 9.9.” $\implies$ “additional affine terms are added to the equations, see §2.1 and Exercise 9.10.”	
2	31	14	$v_i \neq 0 \implies v \neq 0$	AGH
	41	-7	“matrices; then” $\implies$ “matrices; then (in the Euclidean norm)”	
	42	9	(2.30) should be (2.24)	
	42	-10	Insert (2.23) after “By the definition”	
	42	-6	$T(x)^k \implies T^k(x)$	DNK
	43	-14	“more generally.” $\implies$ “when the matrices $A$ and $B$ do not commute.”	
	47	-6	“ <i>fundamental matrix</i> ” $\implies$ “( <i>principal</i> ) <i>fundamental matrix</i> ”	SS
	49	4	$n - k \implies 2m$	AGH
	49	5,6	$u_{k+1}, w_{k+1}, \dots, u_n, w_n \implies u_1, w_1, \dots, u_m, w_m$	
	49	8	$B_k \implies B_1$ AND $B_n \implies B_m$	
	49	9	$B_k \implies B_j$	
	49	11	$C_{k+1} + \dots + C_n \implies C_1 + \dots + C_m$	
	49	-6	$j = k + 1, \dots, n, \implies j = 1, \dots, m$	
	49	-3	$B_k \implies B_1$	
	50	-17	$(T - \lambda_j I)_j^{n_j} v = 0 \implies (T - \lambda_j I)^{n_j} v = 0$	
	56	15	Kronnecker $\implies$ Kronecker	LOJ
	58	7	$Av_3 = 3v_3 \implies Av_3 = 1v_3$	CWW
	58	8	$U = (3) \implies U = (1)$ , $\dot{c}_3 = 3c_3 \implies \dot{c}_3 = 1c_3$	
	58	-15	“One says that” $\implies$ “More precisely, one says that”	SS
	59	12	Add a subscript $k$ : $c_{jlm} \implies c_{jklm}$ and $d_{jlm} \implies d_{jklm}$ . Also $j \in \implies j, k \in$	
	59	12,13	$K/n_s \implies K/n_s^2$ (both lines)	
	63	1,2	“origin is unstable” $\implies$ “zero solution is unstable” (both lines)	SS
	65	-9	“for any linear operator” $\implies$ “for any bounded linear operator”	
66	-6	$M^2 = e^{TR} \implies M^2 = e^{2TR}$	MS	
68	21 (Ex 9c)	“nilpotencies 0,1,2,3.” $\implies$ “nilpotencies 1,2,3.”	KOT	
69	10	$\sum_{i=1}^{n_k} d_{ij} v_j \implies \sum_{j=1}^{n_k} d_{ij} v_j$	AGH	
71	10	“block as in” $\implies$ “blocks as in”		

Chap.	Page	Line	Change	Thanks to
3	76	18-19	“elements of a convergent” $\implies$ “elements of a uniformly convergent”	PJR
	79	4	to the phrase “with the $L_\infty$ norm is complete” append “when E is compact”.	
	86	-15	“complete space $C^0(\mathbb{R}, \mathbb{R}^n)$ ” $\implies$ “complete space $C^0(J, \mathbb{R}^n)$ ”	
	98	Fig 3.7	Vertical axis should be labeled “ $x_o$ ”, not “ $x$ ”	
	99	3	$x : J \rightarrow \mathbb{R}^n \implies x : J \rightarrow E$	
	99	7	$B_b(x_o) \implies B_{b_o}(x_o)$ (Two places!)	
	103	12	In the exponent, $2K$ should be $K$ .	RC
4	110	4	defines a complete flow $\implies$ exists for all $t \in \mathbb{R}$	MS
	110	10	Theorem 3.17 $\implies$ Theorem 3.18	JA
	110	-10	The vector field $F$ defines a flow on $\mathbb{R}^n \implies$ The solutions exist for all $t \in \mathbb{R}$	MS
	111	7	(4.7) $\implies$ (4.8)	
	111	11	and therefore define a flow. $\implies$ and therefore, if $f \in C^1$ , define a flow.	MS
	111	-11	Theorem 3.17 $\implies$ Theorem 3.18	JA
	119	11-12	“be appropriate rely” $\implies$ “be appropriate to rely”	KOT
	121	7	$g(\delta x) = o(\delta x^2) \implies g(\delta x) = O(\delta x^2)$	
	122	8	$y \leq \delta \implies  y  \leq K\delta$	
	122	11	“Let” $\implies$ “Now assume that $ y_o  \leq \delta$ , let”	
	122	11	$ y_o \leq \delta  \implies  y_o  \leq \delta$	
	123	-2	$L(\varphi_t(z)) \implies L(\varphi_s(z))$	
	130	Ftnt 24	“continuous, bijective map that” $\implies$ “continuous, bijective map between compact sets that”	SS
	131	4	“itself, and thus” $\implies$ “itself with a $C^1$ inverse, and thus”	SS
	136	12	“matrices are linearly conjugate” $\implies$ “matrices are similar”	AR
	136	-7	$= (h_2(x_1, x_2) + tx_2) \implies = (h_1(x_1, x_2) + tx_2)$	SS2
	148	-6	“is a subset $M$ of $N$ ” $\implies$ is a neighborhood $M \subset N$	MS
	151	-8	$B_R \subset E \implies B_R \supset E$	
	151	(4.49)	This equation is incorrect. Replace it with	
			$R > \frac{r + \sigma}{2} \begin{cases} 2 & \alpha \leq 2 \\ \frac{\alpha}{\sqrt{\alpha-1}} & \alpha > 2 \end{cases}, \quad \alpha = b \max(1, \sigma^{-1})$	
	151	-5	$R > 38 \implies R > 152/\sqrt{15}$	
	151	-5	$B_{39} \implies B_{40}$	
	152	20	$\frac{d}{dt}(x + y) \implies \frac{d}{dt}(\gamma + y)$	
154	4	$(\partial H/\partial y, \partial H/\partial x) \implies (\partial H/\partial y, -\partial H/\partial x)$		
160	7	“is a unique the equilibrium” $\implies$ “is a unique nonnegative equilibrium”	KOT	
161	7	$\dot{z} = 2z \implies \dot{z} = z$	KLS	
162	-17	$0 \leq z < Z \implies 0 \leq z \leq Z$	KOT	
162	-5	$h(\omega(h^{-1}(y))) \implies h(\omega(h^{-1}(y)))$	KOT	

Chap.	Page	Line	Change	Thanks to	
4	164	7	your systems $\implies$ your system's	KOT	
5	165	-2	"as $t \rightarrow \infty$ " $\implies$ "as $t \rightarrow -\infty$ "	AR	
	174	10	$x(t) = \implies x(t; \sigma) =$		
	176	-1	change the last $ x(t; \sigma) $ to $ x(s; \sigma) $		
	177	-5	$v(t) = v(T) \implies v(t) = u(T)$		
	188	5	$g : E^c \rightarrow E^u \implies g : E^c \rightarrow E^s$		
	188	-1	$F(x, h(x), g(x)) \implies F(x, g(x), h(x))$		
	189	6	$\{(x, h(x), g(x)) : \implies \{(x, g(x), h(x)) :$		
	189	8	$F(x, h(x), g(x)) \implies F(x, g(x), h(x))$		
	190	5	$+\frac{z^4}{16\lambda^2} \implies +\frac{z^4}{16\lambda^3}$		AR
	191	-5	$\{(x_1, x_2, h(x_1, x_2))\} \implies \{(x_1, x_2, g(x_1, x_2))\}$		
	191	-5	$h(x) = \alpha \implies g(x) = \alpha$		
	191	-4	$y = h(x) \implies y = g(x)$		
	191	-3	$\dot{y} = Dh(x) = \frac{\partial h}{\partial x_1} \dot{x}_1 + \frac{\partial h}{\partial x_2} \dot{x}_2$ Replace "h" with "g" in three places		RHG
	192	5	$y = -x_2^2 - x_2^2 \implies y = -x_1^2 - x_2^2$		
	194	10	$\dot{x} = -x + y^2 \implies \dot{x} = -x + xy$		
	194	11	$\dot{y} = 2y + xy \implies \dot{y} = 2y + x^2$		
6	200	-1	$T = 2\pi r^2 \implies T = 2\pi/r^2$	AR AR RM RM	
	212	-4	"a symmetric pair" $\implies$ "a symmetric partner"		
	213	-7	$(y + \alpha x^2 y, -x + \beta y^2 x^2) = -((-y) \implies (-y + \alpha x^2 y, -x - \beta y^2 x^2) = -(-(-y)$		
	222	-14	$\dot{r} = \frac{y^2}{2r} \implies \dot{r} = \frac{y^2}{r}$		
	222	-13	$\dot{r} = -\frac{y^4}{2r} \implies \dot{r} = -\frac{y^4}{r}$		
	224	4	with only one change $\implies$ for $C^2$ flows there is only one change		
	241	Ex. 2.12	Replace the $\dot{x}$ equation with $\dot{x} = x - y - x^2(x + 2y) - xy^2$		
7	252	5	For any functions $\implies$ For any scalar functions	APR	
	256	3	change the $x$ in the 23 element of the matrix (7.21) to $-x$		
	258	-5	and set $v_{ii}(0) \implies$ and set $v_{ij}(0)$		
	262	7	when $\varepsilon < t \implies$ when $\varepsilon < 1$		
	262	-3	$\sum_{m \in \mathbb{Z}^d} \implies \sum_{m \in \mathbb{Z}^d}$	SEO	
	266	2	$< 9 \implies \leq 9$		
	266	3	a Lyapunov basis is $\implies$ an eigenvector basis is		
	266	14	sides of length $1/3 \implies$ sides of length $1/2$		RP

Chap.	Page	Line	Change	Thanks to
8	269	-11	that as $\mu \rightarrow \infty \implies$ that as $\mu \rightarrow -\infty$	SS2
	274	19	$= Dh f(x; p(\nu)) \implies = Dh(x; p(\nu))f(x; p(\nu))$	MS
	279	7	and when $\implies$ and zero when	LOJ
	283	-8	$g(x) = Ax + O(3) \implies g(\xi) = A\xi + O(3)$	LOJ
	283	-4	calls $L_A \implies$ calls $-L_A$	LOJ
	294	Fig 8.9	of (8.49) for $\implies$ of (8.46) for	AA
	294	-7	$b = 1 \implies b = -1$	AA
9	335	-4	$= \int_{U_t} \text{tr}(Df(x(t)))dx \implies = \int_{U_t} \text{tr}(Df(x))dx$	LOJ
	346	- 8	$\frac{dq}{ds} \implies \frac{dq}{ds}(s)$ and $\frac{dt}{ds} \implies \frac{dt}{ds}(s)$	
	368	-5	Hamiltonian flow is $\implies$ Hamiltonian flow on $M_c$ is	LOJ
	369	9	$M_c \implies \theta$	
	350	12	is a $C^2$ diffeomorphism $\implies$ is a $C^2$ embedding	LOJ
	350	-12	$Dh(y) \implies Dh^T(y)$ (in two places) and $D^2h(y)\dot{y} \implies (D^2h(y)\dot{y})^T$	
	350	-11	$Dh(y) \implies Dh^T(y)$	
	361	8	$(2n - 1)n \implies (2n + 1)n$	
	362	4	$(2n - 1)n \implies (2n + 1)n$	
	370	6	$\omega = \pi(I) \implies \omega = \Omega(I)$	
	371	-8	$ m \cdot \omega  > c \implies  m \cdot \omega  \geq c$	
	371	-7	The set $\mathcal{D}_{c,\tau}$ is a $\implies$ The set $\mathcal{D}_{c,\tau} \cap \mathbb{S}^{n-1}$ is a	
	371	-1	$> \frac{d}{ q ^{\tau+1}} \implies \geq \frac{d}{2 q ^{\tau+1}}$	
	372	1	with $d = c/\omega_2 \implies$ with $d = 2c/\omega_2$	
	372	4	$[0, d/2]$ and $[1- \implies [0, d/2)$ and $(1-$	
	372	9	Thus $E$ is bounded $\implies$ Thus $L$ is bounded	
	374	10	$+q^T S q$ , where $S \implies +q^T W q$ where $W$	
	374	-15	two-degrees-of-freedom $\implies$ two degree-of-freedom	
	374	-1	let $Q \implies$ let $\mathcal{Q}$	
	375	7	$\Sigma = \implies S =$	
	387	-14	Casmir $\implies$ Casimir	
	389	5	Exercise 8. $\implies$ (9.39).	
	389	-6	$+ \frac{mga}{I} \implies +2 \frac{mga}{I}$	